

## Mark Scheme (Results)

## Summer 2013

# GCE Further Pure Mathematics 1 (6667/01)





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- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

#### EDEXCEL GCE MATHEMATICS

#### General Instructions for Marking

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes:

- bod benefit of doubt
- ft follow through
- the symbol  $\sqrt[]{}$  will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper
- The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
  - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
  - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.
- 8. In some instances, the mark distributions (e.g. M1, B1 and A1) printed on the candidate's response may differ from the final mark scheme

(But note that specific mark schemes may sometimes override these general principles).

Method mark for solving 3 term quadratic:

1. Factorisation

 $(x^2 + bx + c) = (x + p)(x + q)$ , where |pq| = |c|, leading to x =

 $(ax^2 + bx + c) = (mx + p)(nx + q)$ , where |pq| = |c| and |mn| = |a|, leading to x =

## 2. <u>Formula</u>

Attempt to use <u>correct</u> formula (with values for *a*, *b* and *c*).

### 3. Completing the square

Solving  $x^2 + bx + c = 0$ :  $\left(x \pm \frac{b}{2}\right)^2 \pm q \pm c$ ,  $q \neq 0$ , leading to x = ...

Method marks for differentiation and integration:

1. Differentiation

Power of at least one term decreased by 1. (  $x^n \rightarrow x^{n-1}$  )

### 2. Integration

Power of at least one term increased by 1. (  $x^n \rightarrow x^{n+1}$  )

Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

<u>Method mark</u> for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.

Where the formula is <u>not</u> quoted, the method mark can be gained by implication from <u>correct</u> working with values, but may be lost if there is any mistake in the working.

Exact answers

Examiners' reports have emphasised that where, for example, an <u>exact</u> answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

### Answers without working

The rubric says that these  $\underline{may}$  not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required.

Question Number	Scheme	Notes	Marks
1.	$\mathbf{M} = \begin{pmatrix} x & x-2\\ 3x-6 & 4x-11 \end{pmatrix}$		
	$det \mathbf{M} = x(4x - 11) - (3x - 6)(x - 2)$ Correct attempt at determinant		M1
	$x^2 + x - 12$ (=0)	Correct 3 term quadratic	A1
	$(x+4)(x-3) (= 0) \rightarrow x =$	Their $3TQ = 0$ and attempts to solve relevant quadratic using factorisation or completing the square or correct quadratic formula leading to $x =$	M1
	x = -4, x = 3	Both values correct	A1
			(4)
			Total 4
Notes			
	x(4x-11) = (3x-6)(x-2) award first M1		
	$\pm (x^2 + x - 12)$ seen award first M1A1		
	Method mark for solving 3 term quadratic: 1. <u>Factorisation</u> $(x^2 + bx + c) = (x + p)(x + q)$ , where $ pq  =  c $ , leading to $x =$ $(ax^2 + bx + c) = (mx + p)(nx + q)$ , where $ pq  =  c $ and $ mn  =  a $ , leading to $x =$ 2. <u>Formula</u> Attempt to use <u>correct</u> formula (with values for <i>a</i> , <i>b</i> and <i>c</i> ). 3. <u>Completing the square</u> Solving $x^2 + bx + a = 0$ ; $(x + b)^2 + a + a = a \neq 0$ , leading to $x =$		
	Both correct with no working 4/4, only one correct 0/4		

Question Number	Scheme	Notes	Marks
2	$f(x) = \cos\left(x^2\right)$	$(x^2) - x + 3$	
(a)	f(2.5) = 1.499 f(3) = -0.9111	Either any one of $f(2.5) = awrt 1.5$ or f(3) = awrt -0.91	M1
	<b>Sign change (positive, negative)</b> (and $f(x)$ is continuous) therefore root or equivalent.	Both $f(2.5) = awrt 1.5$ and $f(3) = awrt -0.91$ , sign change and conclusion.	A1
	Use of degrees gives $f(2.5) = 1.494$ and $f(3) = 0.988$ which is awarded M1A0		
(b)	$\frac{3-\alpha}{"0.91113026188"} = \frac{\alpha - 2.5}{"1.4994494182"}$	Correct linear interpolation method – accept equivalent equation - ensure signs are correct.	M1 A1ft
	$\alpha = \frac{3 \times 1.499 + 2.5 \times 0.9111}{1.499 + 0.9111}$		
	$\alpha = 2.81  (2d.p.)$	cao	A1
			(3)
			Total 5
Notes	Alternative (b)		
	Gradient of line is $-\frac{'1.499'+'0.9111'}{0.5}$ (= -4.82) (3sf). Attempt to find equation of		
	straight line and equate y to 0 award M1 and A1ft for their gradient awrt 3sf.		

Question Number	Scheme	Notes	Marks
3(a)	Ignore part labels and mark part (a) and part (b) together.		
	$f\left(\frac{1}{2}\right) = 2\left(\frac{1}{2}\right)^3 - 9\left(\frac{1}{2}\right)^2 + k\left(\frac{1}{2}\right) - 13$	Attempts f(0.5)	M1
	$\left(\frac{1}{4}\right) - \left(\frac{9}{4}\right) + \left(\frac{k}{2}\right) - 13 = 0 \Longrightarrow k = \dots$	Sets $f(0.5) = 0$ and leading to $k=$	dM1
	k = 30	cao	A1
	Alternative using	long division:	
	$2x^3 - 9x^2 + kx - 13 \div (2x - 1)$		
	$= x^{2} - 4x + \frac{1}{2}k - 2$ (Quotient)	Full method to obtain a remainder as a function of $k$	M1
	Remainder $\frac{1}{2}k - 15$		
	$\frac{1}{2}k - 15 = 0$	Their remainder $= 0$	dM1
	k = 30 Alternative by inspection:		A1
		First M for $(2x-1)(x^2+bx+c)$ or	
	$(2x-1)(x^2-4x+13) = 2x^3-9x^2+30x-13$	$(x-\frac{1}{2})(2x^2+bx+c)$	M1dM1
		Second M1 for $ax^2 + bx + c$ where ( $b = -4$ or $c = 13$ )or ( $b = -8$ or $c = 26$ )	
	k = 30		A1
			(3)
(b)	$f(x) = (2x-1)(x^2 - 4x + 13)$ or $\left(x - \frac{1}{2}\right)(2x^2 - 8x + 26)$	M1: $(x^2 + bx \pm 13)$ or $(2x^2 + bx \pm 26)$ Uses inspection or long division or compares coefficients <b>and</b> $(2x - 1)$ or $\left(x - \frac{1}{2}\right)$ to obtain a quadratic factor of this form.	M1
	$x^2 - 4x + 13$ or $2x^2 - 8x + 26$	A1 $(x^2 - 4x + 13)$ or $(2x^2 - 8x + 26)$ seen	A1
	$x = \frac{4 \pm \sqrt{4^2 - 4 \times 13}}{2}$ or equivalent	Use of correct quadratic formula for their $\underline{3TQ}$ or completes the square.	M1
	$x = \frac{4 \pm 6i}{2} = 2 \pm 3i$	oe	A1
			(4)
			Total 7

Question Number	Scheme	Notes	Marks
4(a)	$y = \frac{4}{x} = 4x^{-1} \implies \frac{dy}{dx} = -4x^{-2} = -\frac{4}{x^2}$	$\frac{\mathrm{d}y}{\mathrm{d}x} = k x^{-2}$	
	$xy = 4 \Longrightarrow x \frac{\mathrm{d}y}{\mathrm{d}x} + y = 0$	Use of the product rule. The sum of two terms including $dy/dx$ , one of which is correct.	M1
	$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{\mathrm{d}y}{\mathrm{d}t} \cdot \frac{\mathrm{d}t}{\mathrm{d}x} = -\frac{2}{t^2} \cdot \frac{1}{2}$	their $\frac{dy}{dt} \times \left(\frac{1}{\text{their}\frac{dx}{dt}}\right)$	
	$\frac{dy}{dx} = -4x^{-2} \text{ or } x \frac{dy}{dx} + y = 0 \text{ or } \frac{dy}{dx} = -\frac{2}{t^2} \cdot \frac{1}{2}$ or equivalent expressions	Correct derivative $-4x^{-2}$ , $-\frac{y}{x}$ or $\frac{-1}{t^2}$	A1
	So, $m_N = t^2$	Perpendicular gradient rule $m_N m_T = -1$	M1
	$y - \frac{2}{t} = t^2 \left( x - 2t \right)$	$y - \frac{2}{t}$ = their $m_N (x - 2t)$ or $y = mx + c$ with their $m_N$ and $(2t, \frac{2}{t})$ in an attempt to find 'c'. Their gradient of the normal must be different from their gradient of the tangent and have come from calculus and should be a function of t.	M1
	$ty - t^3 x = 2 - 2t^4  *$		A1* cso
			(5)
(b)	$t = -\frac{1}{2} \Longrightarrow -\frac{1}{2} y - \left(-\frac{1}{2}\right)^3 x = 2 - 2\left(-\frac{1}{2}\right)^4$	Substitutes the given value of <i>t</i> into the normal	M1
	4y - x + 15 = 0		
	$y = \frac{4}{x} \Longrightarrow x^2 - 15x - 16 = 0 \text{ or}$ $\left(2t, \frac{2}{t}\right) \rightarrow \frac{8}{t} - 2t + 15 = 0 \Longrightarrow 2t^2 - 15t - 8 = 0 \text{ or}$ $x = \frac{4}{y} \Longrightarrow 4y^2 + 15y - 4 = 0.$	Substitutes to give a quadratic	M1
	$(x+1)(x-16) = 0 \Rightarrow x = \text{ or}$ $(2t+1)(t-8) = 0 \Rightarrow t = \text{ or}$ $(4y-1)(y+4) = 0 \Rightarrow y =$	Solves their 3TQ	M1
	$(P: x = -1, y = -4)(Q:)x = 16, y = \frac{1}{4}$	Correct values for <i>x</i> and <i>y</i>	A1
			(4) Total 9

Question Number	Scheme	Notes	Marks
5(a)	$(r+2)(r+3) = r^2 + 5r + 6$		B1
	$\sum \left( r^2 + 5r + 6 \right) = \frac{1}{6} n \left( n + 1 \right) \left( 2n + 1 \right) + 5 \times \frac{1}{2} n \left( n + 1 \right), +6n$	M1: Use of correct expressions for $\sum r^2$ and $\sum r$ B1ft: $\sum k = nk$	M1,B1ft
	$=\frac{1}{3}n\left[\frac{1}{2}(n+1)(2n+1)+\frac{15}{2}(n+1)+18\right]$	M1:Factors out <i>n</i> ignoring treatment of constant. A1: Correct expression with $\frac{1}{3}n$ or $\frac{1}{6}n$ factored out, allow recovery.	M1 A1
	$\left( = \frac{1}{3}n \left[ n^2 + \frac{3}{2}n + \frac{1}{2} + \frac{15}{2}n + \frac{15}{2} + 18 \right] \right)$ $= \frac{1}{3}n \left[ n^2 + 9n + 26 \right] *$	Correct completion to printed answer	A1*cso
			(6)
5(b)	$\sum_{r=n+1}^{3n} = \frac{1}{3} 3n \Big( (3n)^2 + 9(3n) + 26 \Big) - \frac{1}{3} n \Big( n^2 + 9n + 26 \Big)$	M1: $f(3n) - f(n \text{ or } n+1)$ and attempt to use part (a). A1: Equivalent correct expression	M1A1
	3f(n) - f(n  or  n+1) is M0		
	$(=n(9n^{2}+27n+26)-\frac{1}{3}n(n^{2}+9n+26))$		
	$=\frac{2}{3}n\left(\frac{27}{2}n^2+\frac{81}{2}n+39-\frac{1}{2}n^2-\frac{9}{2}n-13\right)$	Factors out $=\frac{2}{3}n$ dependent on previous M1	dM1
	$=\frac{2}{3}n(13n^2+36n+26)$	Accept correct expression.	A1
	(a = 13, b = 36, c = 26)		
			(4)
			Total 10

Question Number	Scheme	Notes	Marks
6(a)	$y = 2a^{\frac{1}{2}}x^{\frac{1}{2}} \Longrightarrow \frac{dy}{dx} = a^{\frac{1}{2}}x^{-\frac{1}{2}}$	$x^{\frac{1}{2}} \to x^{-\frac{1}{2}}$	
	$y^2 = 4ax \Longrightarrow 2y \frac{dy}{dx} = 4a$	$ky\frac{\mathrm{d}y}{\mathrm{d}x} = c$	M1
	or $\frac{dy}{dx} = \frac{dy}{dt} \cdot \frac{dt}{dx} = 2a \cdot \frac{1}{2ap}$	$\frac{\mathrm{d}y}{\mathrm{d}t} \times \frac{1}{\frac{\mathrm{d}x}{\mathrm{d}t}}$ . Can be a function of <i>p</i> or <i>t</i> .	
	$\frac{\mathrm{d}y}{\mathrm{d}x} = a^{\frac{1}{2}}x^{-\frac{1}{2}} \text{ or } 2y\frac{\mathrm{d}y}{\mathrm{d}x} = 4a \text{ or } \frac{\mathrm{d}y}{\mathrm{d}x} = 2a.\frac{1}{2ap}$	Differentiation is accurate.	A1
		Applies $y - 2ap = \text{their } m(x - ap^2)$	
	$1 (r - r^2)$	or $y = (\text{their } m)x + c$ using	141
	y - 2ap = -(x - ap)	$x = ap^2$ and $y = 2ap$ in an attempt to find	MI
		<i>c</i> . Their <i>m</i> must be a function of <i>p</i> from calculus.	
	$py - x = ap^2 *$	Correct completion to printed answer*	A1 cso
			(4)
(b)	$qy - x = aq^2$		B1
			(1)
( <b>c</b> )	$qy - aq^2 = py - ap^2$	Attempt to obtain an <b>equation</b> in one variable <i>x</i> or <i>y</i>	M1
	$y(q-p) = aq^2 - ap^2$		
	$y = \frac{aq^2 - ap^2}{q - p}$	Attempt to isolate <i>x</i> or <i>y</i>	M1
	y = a(p+q) or ap + aq x = apq	A1: Either one correct simplified coordinate A1: Both correct simplified coordinates	A1,A1
	(R(apq, ap + aq))		
( <b>d</b> )			(4)
(u)	' <i>apq</i> '=- <i>a</i>	Their <i>x</i> coordinate of $R = -a$	M1
	pq = -1	Answer only: Scores $2/2$ if x coordinate of R is apq otherwise $0/2$ .	A1
			(2)
			1 otal 11

Question Number	Scheme	Notes	Marks
7	$z_1 = 2 + 3i,  z_2 = 3 + 2i$		
(a)	$z_1 + z_2 = 5 + 5i \implies  z_1 + z_2  = \sqrt{5^2 + 5^2}$	Adds $z_1$ and $z_2$ and correct use of Pythagoras. i under square root award M0.	M1
	$\sqrt{50} \ (= 5\sqrt{2})$		A1 cao
			(2)
(b)	$\frac{z_1 z_3}{z_2} = \frac{(2+3i)(a+bi)}{3+2i}$	Substitutes for $z_1, z_2$ and $z_3$ and multiplies	
	$=\frac{(2+3i)(a+bi)(3-2i)}{(3+2i)(3-2i)}$	by $\frac{3-2i}{3-2i}$	M1
	(3+2i)(3-2i) = 13	13 seen.	B1
	$\frac{z_1 z_3}{z_2} = \frac{(12a - 5b) + (5a + 12b)i}{13}$	M1: Obtains a numerator with 2 real and 2 imaginary parts. A1: As stated or $\frac{(12a-5b)}{13} + \frac{(5a+12b)}{13}i$ ONLY.	dM1A1
		~	(4)
(c)	12a - 5b = 17 $5a + 12b = -7$	compares real and imaginary parts to obtain 2 equations which both involve <i>a</i> and <i>b</i> . Condone sign errors only.	M1
	$\begin{array}{l} 60a - 25b = 85\\ 60a + 144b = -84 \end{array} \implies b = -1 \end{array}$	Solves as far as $a = \text{ or } b =$	dM1
	a = 1, b = -1	Both correct	A1
		Correct answers with no working award 3/3.	
			(3)
( <b>d</b> )	$\arg(w) = -\tan^{-1}\left(\frac{7}{17}\right)$	Accept use of $\pm \tan^{-1}$ or $\pm \tan$ . awrt $\pm 0.391$ or $\pm 5.89$ implies M1.	M1
	=awrt - 0.391 or awrt 5.89		A1
			(2)
			Total 11

Question Number	Scheme	Notes	Marks
<b>8</b> (a)	$\mathbf{A}^{2} = \begin{pmatrix} 6 & -2 \\ -4 & 1 \end{pmatrix} \begin{pmatrix} 6 & -2 \\ -4 & 1 \end{pmatrix} = \begin{pmatrix} 44 & -14 \\ -28 & 9 \end{pmatrix}$	M1:Attempt both $\mathbf{A}^2$ and $7\mathbf{A} + 2\mathbf{I}$	
	$7\mathbf{A} + 2\mathbf{I} = \begin{pmatrix} 42 & -14 \\ -28 & 7 \end{pmatrix} + \begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix} = \begin{pmatrix} 44 & -14 \\ -28 & 9 \end{pmatrix}$	A1: Both matrices correct	M1A1
	$OR \mathbf{A}^2 - 7\mathbf{A} = \mathbf{A} (\mathbf{A} - 7\mathbf{I})$	M1 for expression and attempt to substitute and multiply (2x2)(2x2)=2x2	
	$\mathbf{A} \left( \mathbf{A} - 7\mathbf{I} \right) = \begin{pmatrix} 6 & -2 \\ -4 & 1 \end{pmatrix} \begin{pmatrix} -1 & -2 \\ -4 & -6 \end{pmatrix} = \begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix} = 2\mathbf{I}$	A1 cso	
			(2)
(b)	$\mathbf{A}^2 = 7\mathbf{A} + 2\mathbf{I} \Longrightarrow \mathbf{A} = 7\mathbf{I} + 2\mathbf{A}^{-1}$	Require one correct line using accurate expressions involving $A^{-1}$ and identity matrix to be clearly stated as I.	M1
	$\mathbf{A}^{-1} = \frac{1}{2} \left( \mathbf{A} - 7\mathbf{I} \right)^{*}$		A1* cso
	Numerical approach award 0/2.		
			(2)
(c)	$\mathbf{A}^{-1} = \frac{1}{2} \begin{pmatrix} -1 & -2 \\ -4 & -6 \end{pmatrix}$	Correct inverse matrix or equivalent	B1
	$\frac{1}{2} \begin{pmatrix} -1 & -2 \\ -4 & -6 \end{pmatrix} \begin{pmatrix} 2k+8 \\ -2k-5 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} -2k-8+4k+10 \\ -8k-32+12k+30 \end{pmatrix}$	Matrix multiplication involving their inverse and k: (2x2)(2x1)=2x1. N.B. $\begin{pmatrix} 6 & -2 \\ -4 & 1 \end{pmatrix} \begin{pmatrix} 2k+8 \\ -2k-5 \end{pmatrix}$ is M0	M1
	$\binom{k+1}{2k-1} \text{ or } (k+1, 2k-1)$	(k+1) first A1, $(2k-1)$ second A1	A1,A1
	Or:		
	$\begin{pmatrix} 6 & -2 \\ -4 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 2k+8 \\ -2k-5 \end{pmatrix}$	Correct matrix equation.	B1
	6x - 2y = 2k + 8 -4x + y = -2k - 5 $\Rightarrow$ x = or y =	Multiply out and attempt to solve simultaneous equations for $x$ or $y$ in terms of $k$ .	M1
	$\binom{k+1}{2k-1} \text{ or } (k+1, 2k-1)$	(k+1) first A1, $(2k-1)$ second A1	A1,A1
			(4)
			Total 8

Question Number	Scheme	Notes	Marks
9(a)	$u_1 = 8$ given $n = 1 \Longrightarrow u_1 = 4^1 + 3(1) + 1 = 8$ (: true for $n = 1$ )	$4^1 + 3(1) + 1 = 8$ seen	B1
	Assume true for $n = k$ so that $u_k = 4^k + 3k + 1$		
	$u_{k+1} = 4(4^k + 3k + 1) - 9k$	Substitute $u_k$ into $u_{k+1}$ as $u_{k+1} = 4u_k - 9k$	M1
	$= 4^{k+1} + 12k + 4 - 9k = 4^{k+1} + 3k + 4$	Expression of the form $4^{k+1} + ak + b$	A1
	$=4^{k+1}+3(k+1)+1$	Correct completion to an expression in terms of $k + 1$	A1
	If <u>true for <math>n = k</math> then true for <math>n = k + 1</math> and as true for <math>n = 1</math> true for all <math>n</math></u>	Conclusion with all 4 underlined elements that can be seen anywhere in the solution; <i>n</i> defined incorrectly award A0.	A1 cso
			(5)
(b)	Condone use of <i>n</i> here.		
	$lhs = \begin{pmatrix} 3 & -4 \\ 1 & -1 \end{pmatrix} = \begin{pmatrix} 3 & -4 \\ 1 & -1 \end{pmatrix}$ $rhs = \begin{pmatrix} 2(1)+1 & -4(1) \\ 1 & 1-2(1) \end{pmatrix} = \begin{pmatrix} 3 & -4 \\ 1 & -1 \end{pmatrix}$	Shows true for $m = 1$	B1
	Assume $\begin{pmatrix} 3 & -4 \\ 1 & -1 \end{pmatrix}^k = \begin{pmatrix} 2k+1 & -4k \\ k & 1-2k \end{pmatrix}$		
	$ \begin{pmatrix} 3 & -4 \\ 1 & -1 \end{pmatrix}^{k+1} = \begin{pmatrix} 2k+1 & -4k \\ k & 1-2k \end{pmatrix} \begin{pmatrix} 3 & -4 \\ 1 & -1 \end{pmatrix} $	$ \begin{pmatrix} 3 & -4 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} 2k+1 & -4k \\ k & 1-2k \end{pmatrix} $ award M1	M1
	$= \begin{pmatrix} 6k+3-4k & -8k-4+4k \\ 3k+1-2k & -4k-1+2k \end{pmatrix}$	Or equivalent 2x2 matrix. $ \begin{pmatrix} 6k+3-4k & -12k-4+8k \\ 2k+1-k & -4k-1+2k \end{pmatrix} $ award A1from above.	A1
	$= \left( \begin{pmatrix} 2k+3 & -4k-4\\ k+1 & -2k-1 \end{pmatrix} \right)$		
	$= \begin{pmatrix} 2(k+1)+1 & -4(k+1) \\ k+1 & 1-2(k+1) \end{pmatrix}$	Correct completion to a matrix in terms of $k + 1$	A1
	If <u>true for <math>m = k</math> then true for <math>m = k + 1</math> and as true for <math>m = 1</math> true for all <math>m</math></u>	Conclusion with all 4 underlined elements that can be seen anywhere in the solution; <i>m</i> defined incorrectly award A0.	A1 cso
			(5) Total 10
			1.0001.10

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